



Engineering self-sustaining networks:
resolving the paradox

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Westerhoff and Heijmans, Oxford, 20100712

Synthetic biology

Making Life
Changing Life
for a purpose


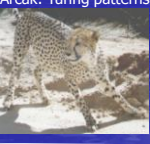
**Always: stick molecules into
sufficient networks**

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What is Life?

- A self-sustaining (stubborn) system
 - Repair or duplication
 - Gibbs energy dissipation
 - Labile structure
 - Heterogeneity & symmetry breaking beyond statistical thermodynamics

Arcak: Turing patterns

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Engineering the self-sustaining networks

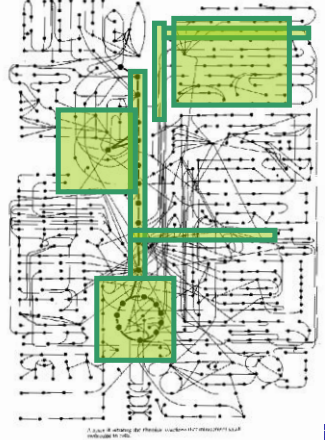
- Self-sustaining cell may not worry about efficiency
- How does the cell engineer itself
- Synthetic biology: microsurgery
- Noise and heterogeneity beyond the thermodynamic limit
- Towards synthetic biology of heterogeneous cross-talk

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Our first objective for synthetic biology:

a dynamic model
of a metabolic **chassis**
to facilitate synthetic biology

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- **Chassis**
- Pathways that manage the large fluxes essential for the conserved properties and Gibbs energy:
- First: carbon and energy metabolism

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linlog approximation of kinetics

Detailed, fully annotated, compartmentalized kinetic model

Medium throughput protein purification

Miniature enzyme assay

Absolute concentrations in endometabolome and exometabolome

Absolute quantification of enzymes using QconCAT

Integrating data and software resources

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Engineering self-sustaining networks

Michael hecht: Life is special

It is, hence:
An example of self-sustaining network-based complexity:
lack of interest in efficiency

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glycerol

-2 ATP

alcohol

2 ATP

CO₂ only

36 ATP

Flux balance analysis

Does yeast engage the most efficient route (??)

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Summary of exometabolomics:
Not the maximal efficiency route

Flux	Flux percentage of input
J_{Biomass}	6
J_{CO_2} (offgas)	20
J_{ethanol} (exometabolome plus off gas)	74
J_{Acetate} (exometabolome)	0
J_{Glycerol} (exometabolome)	2
$J_{\text{Acetaldehyde}}$ (exometabolome)	0
$J_{\text{Trehalose}}$ (exometabolome)	1

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Flux	Flux (mmoles C/h/g dryweight)	Flux percentage of input
J_{Biomass}		6
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Engineering self-sustaining networks

Neither maximally efficient
Nor simplest

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Engineering self-sustaining networks

Engineering the self-sustaining networks

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Engineering strategy for a network

- Engineer the most controlling step?
- Or
- Do what the organism does? Or at least learn from this.

How to identify the strongest controller?

experimentally or *in silico*

The Flux Control Coefficient

$$C_i^J = \left(\frac{d \ln |J|}{d \ln e_i} \right)_{\text{steady state}} = \frac{dJ/J}{de_i/e_i} = \frac{\%dJ}{1\%de_i}$$

Flux versus enzyme activity

Flux control distribution *ex silico*:

Enzyme	C_i^J	Notes
GLT	0.97	High control confirmed experimentally, though indirectly
HK	0.15	
PGI	0.00	
PFK	0.00	
ALD	0.00	
TPI		
GAPDH	0.01	
PGK	0.00	

Should we just engineer this step, or should we perhaps try to learn from the Biology?

Does the organism re-engineer itself by modulating the step with the highest control on the flux?

For: Control \neq Regulation

Control: what limits a flux

Regulation: what the cell actually does to change the flux

The cell invokes gene expression: adaptation

Straightforward strategies for regulation of **pathway flux**

Does the cell only regulate the step with highest control?
or
Does the cell regulate flux by reducing all enzyme levels equally?

Regulation analysis:
How much of function is regulated by gene expression, how much metabolically?

$$v = v(e, X) = e \cdot v(X)$$

Gene expression \rightarrow e \rightarrow $v(X)$ (Metabolic/direct)

$$\rho_h \equiv \frac{\Delta \ln e}{\Delta \ln J} \cong \frac{\text{fold change in amount of enzyme}}{\text{fold change of flux through it}}$$

Average over a larger number of studies

Enzyme	ρ_h	Standard deviation
HK2	0.0	0.9
HK1	0.3	0.6
PGI		
PFK		
ALD		
TPI		
GAPDH		
PGK		
GPW		
ENO		
PKY		
PDC		
ADH		
Overall		

Not the high control step!

Enzyme	ρ_h	Notes
GLT	0.97	High control confirmed experimentally, though indirectly
HK	0.15	
PGI	0.00	
PFK	0.00	
ALD	0.00	
TPI		
GAPDH	0.01	
PGK	0.00	

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Strategies of regulation of pathway flux

Does the cell only ~~X~~ regulate the step with highest control?
or
Does the cell regulate flux by reducing all enzyme levels equally?

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If homogeneous regulation

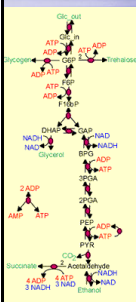
- System Biology laws

$$C_1^J + C_2^J + C_3^J + \dots + C_n^J = 1$$

- If all ρ_h 's equal to each other

$$(C_1^J + C_2^J + C_3^J + \dots + C_n^J) \cdot \rho_h = 1$$

- then:

$$\rho_h = 1$$


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Is Regulation homogeneous (the entire network equally)?

Nitrogen starvation	ρ_h
HK	1.0
PGI	0.8
PFK	0.4
ALD	1.1
TPI	0.1
GAPDH	0.7
PGK	0.0
PGM	1.0
ENO	0.4
PK	1.4
PDC	2.3
ADH	1.7

No!!

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Does the living cell use the straightforward strategies for regulation of pathway flux?

Does the cell only ~~X~~ regulate the step with highest control?
or
Does the cell regulate flux by reducing all enzyme levels equally?

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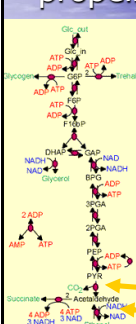
Neither of the obvious strategies is used by the cell

Rather: a more sophisticated strategy

Propeller enzymes/genes: $\rho_{h,i} > 1 \Rightarrow \rho_{h,j} < 0$

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Regulation understood: propeller enzymes and followers



Nitrogen starvation	ρ_h
HK	1.0
PGI	0.8
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New engineering strategy?

Identify and then activate the propeller enzymes, i.e. use the regulation of the cell itself:
A different kind of Control Theory (cf. Murat Arcaik):
Engineering self-sustaining systems

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Engineering the self-sustaining networks

- Self-sustaining cell may not worry about efficiency
- How does the cell engineer itself
- **Synthetic biology: microsurgery**
- Noise and heterogeneity beyond the thermodynamic limit
- Towards synthetic biology of heterogeneous cross-talk

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Synthetic Biology

The microsurgery method

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Engineering self-sustaining systems

Such that they do not notice:
– Keep metabolite concentrations the same

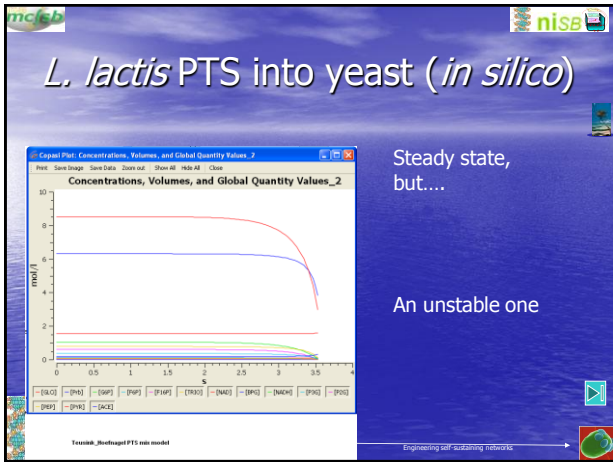
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The principle *in silico*: balance the fluxes with expression levels

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Yeast HXT+HXK into *L. lactis* (*in silico*)

A steady state indeed



- ### *In silico* microsurgery for synthetic biology:
- Stability requires additional regulatory loops
 - Criterion: real part of eigenvalue with positive real part

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-

The steady consequences of dynamic noise

Cell-cell heterogeneity
Pattern formation

Living systems may expend Gibbs free energy to stay heterogeneous

but how?

Non-equilibrium metabolic noise might be generated by gene expression

Dependence of Protein Noise on Rates

```

    graph TD
      DNA[DNA] -- 1 --> mRNA[mRNA]
      mRNA -- 2 --> Protein[Protein]
      DNA -- 3 --> Protein
  
```

Dependence of Protein Noise on Gene expression noise

```

    graph TD
      DNA[DNA] -- 1 --> mRNA[mRNA]
      mRNA -- 2 --> Protein[Protein]
      DNA -- 3 --> Protein
  
```

Fast mRNA reactions

1 = 5*DNA 2 = 1*mRNA
3 = 0.5*mRNA 4 = 0.1*prot

Equal mRNA & protein reactions

1 = 0.5*DNA 2 = 0.1*mRNA
3 = 0.5*mRNA 4 = 0.1*prot

Fast protein reactions

1 = 0.5*DNA 2 = 0.1*mRNA
3 = 5*mRNA 4 = 5*prot

Thermodynamic view

Noise can contain Gibbs free energy

Equilibrium noise is limited in magnitude

$$\sigma^2(N) = \bar{N}$$

$$\frac{\sigma(N)}{\bar{N}} = \frac{1}{\sqrt{\bar{N}}}$$

$$\frac{\sigma(4)}{4} = 0.5$$

$$\frac{\sigma(1000)}{1000} = 0.01$$

$$\text{Fano factor } \phi = \frac{\sigma^2(N)}{\bar{N}} = 1 \text{ at equilibrium}$$

$\phi \gg 1?$

```

    graph TD
      DNA[DNA] -- 1 --> mRNA[mRNA]
      mRNA -- 2 --> Protein[Protein]
      DNA -- 3 --> Protein
  
```

Fast mRNA reactions

1 = 5*DNA 2 = 1*mRNA
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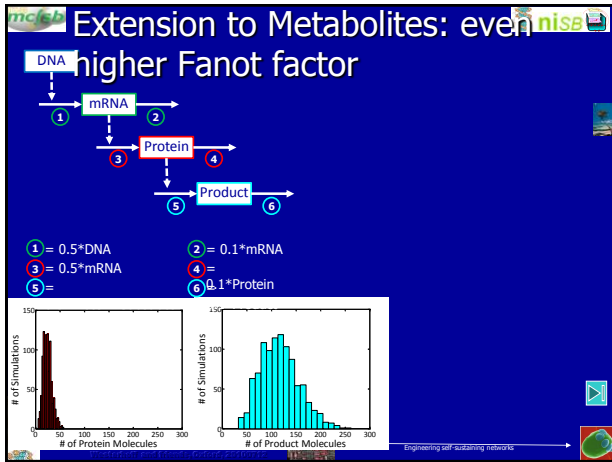
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1 = 0.5*DNA 2 = 0.1*mRNA
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Fast protein reactions

1 = 0.5*DNA 2 = 0.1*mRNA
3 = 5*mRNA 4 = 5*prot

Reaction Condition	mRNA Fano Factor (σ^2/μ)	Protein Fano Factor (σ^2/μ)
Fast mRNA reactions	0.9999	1.323
Equal mRNA & protein reactions	1.0004	3.6746



Metabolic noise exceeding the thermodynamic limit through gene expression hierarchy

Step towards diversity and robustness?

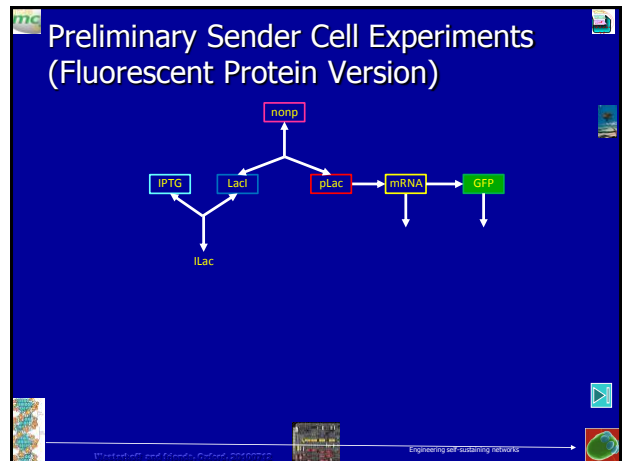
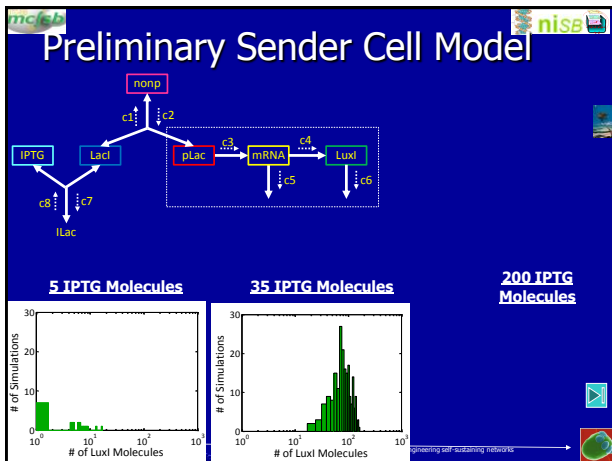
Implications for synthetic biology of patterns

- Non-Poisson distribution proves mechanism to reach heterogeneity beyond triviality
- Engineering the required noise characteristics

See also poster by Vicky Jackson

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Higher diversity than with the simple model

Self-sustaining networks are amplifying?

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Engineering the self-sustaining networks

- Self-sustaining cell may not worry about efficiency 😊
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- Noise and heterogeneity beyond the thermodynamic limit 😊
- Towards synthetic biology of heterogeneous cross-talk 😊

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FEBSX-SysBio 2011

We cordially invite you to the

Joint FEBS/Systems X **Advanced Lecture Course** on
Systems Biology – From Molecules to Function
 26 February 2011 – 3 March 2011: Innsbruck, Austria, EU
<http://www.febssysbio.net/>

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